

# A Tight Scrutiny Of Electroweak Phase Transitions

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Based on  $1511 \pm 1.xxxxx$  with David Curtin & Patrick Meade

# Baryogenesis problem

- Fact: The universe around us has excess matter over antimatter
- Baryon-Antibaryon asymmetry with symmetric initial conditions.
- Sakharov Conditions:
  1. C&CP violation
  2. B violating processes
  3. Thermal inequilibrium

# Finite Temperature Effective Potential

- Need Effective Potential  $V$  to talk about vev as its minimum.
- Tree level  $V$  gets corrections at 1-loop
- Captured by Coleman-Weinberg calculation
- Finite temperature: virtual interactions with plasma
- Imaginary Time formalism to modify potential

# 10 second crash course in FTFT

$$V_{CW} = \frac{1}{2} \int \frac{d^4 k}{(2\pi)^4} \text{Log}[k_E^2 + M^2]$$

Good old CW potential

$$\int \frac{dk_4}{2\pi} f(k_4) \rightarrow T \sum_n f(k_4 = i\omega_n), \omega_n = 2\pi nT$$

Imaginary time formalism  
replacement

$$V_{CW} = V_{CW}^{T=0} + V_{CW}^{T \neq 0}$$

Splits neatly into T-dependent  
and T-independent parts

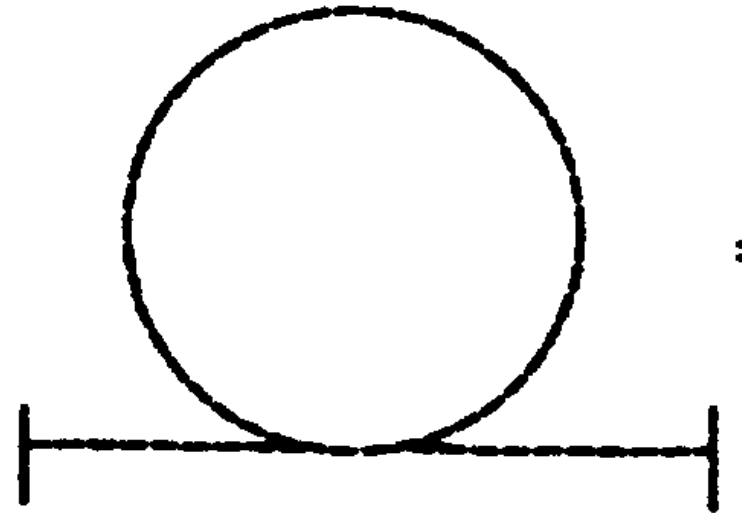
$$V_{CW}^{T \neq 0} = \frac{T}{2\pi^2} \int dp p^2 \log[1 - \exp[-\beta \sqrt{p^2 + M^2}]]$$

# Break down of P.T :Conventional wisdom

$$V_{CW}^{T \neq 0} = \frac{T^4}{2\pi^2} J_B\left(\frac{M^2}{T^2}\right)$$

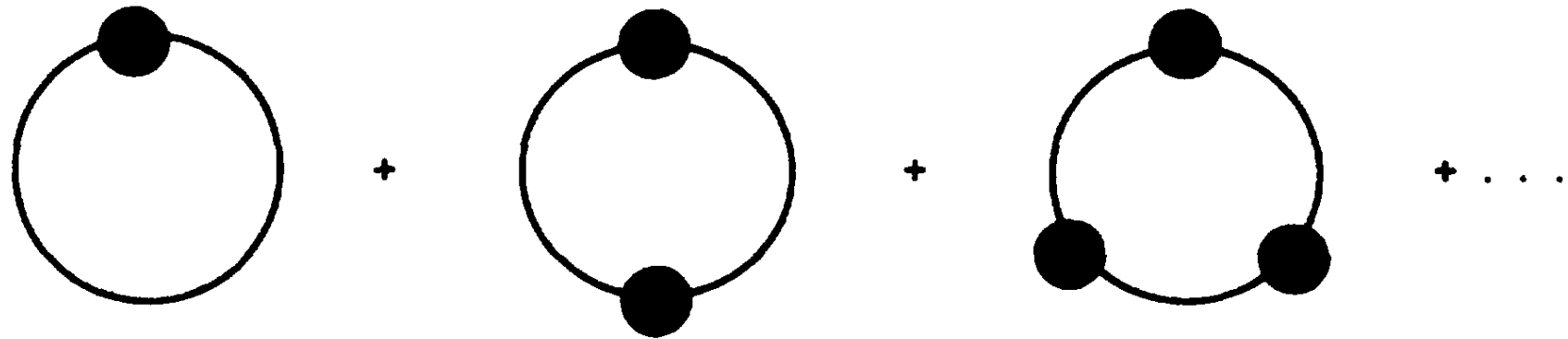
In the high T limit,

$$\Pi_1(T) = \frac{d^2 V_{CW}^{T \neq 0}}{dh^2} = \frac{\lambda}{4} T^2$$

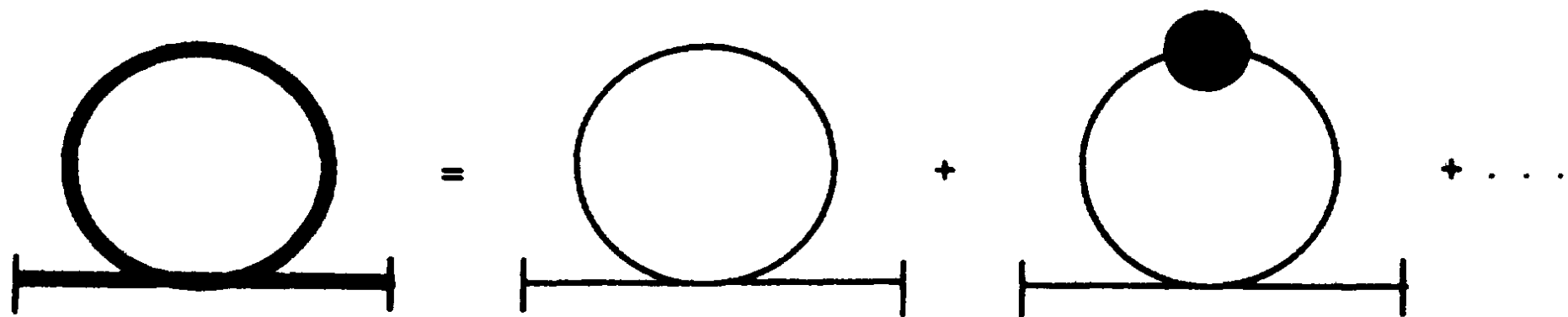


- the one loop generated thermal mass is much larger than the tree level mass.
- Break down in P.T.

# Ring Terms



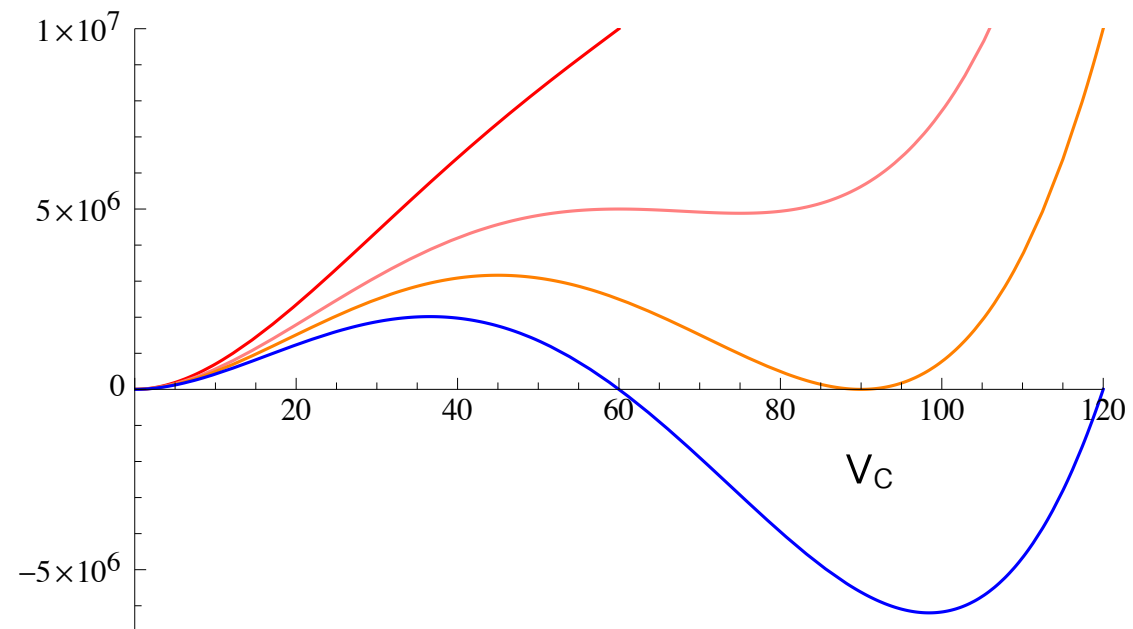
- contributions from all orders (called Daisy diagrams).
- to resum Daisies, replace  $M^2 \rightarrow M^2 + \Pi$



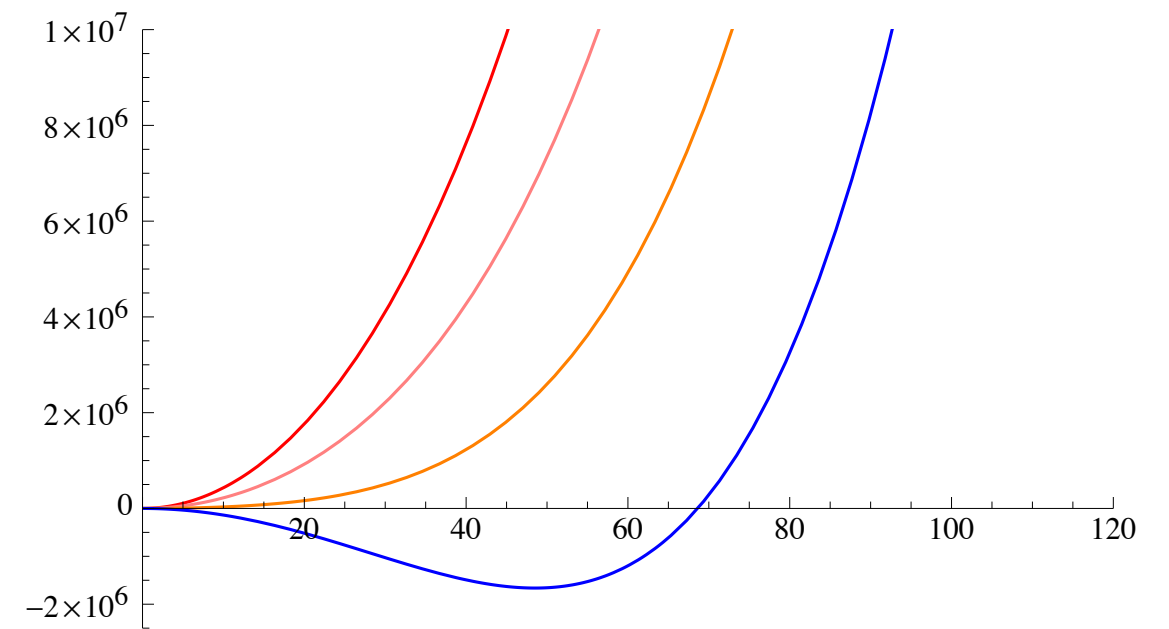
# Incapable standard model

- Not enough CP violation
- Could EWSB( $h=0 \rightarrow h=v$ ) provide thermal in-equilibrium?
- Phase transition required to be first order to prevent Baryon washout
- Standard model provides only second order phase transition

# Cooling Down



1st order Phase Transition



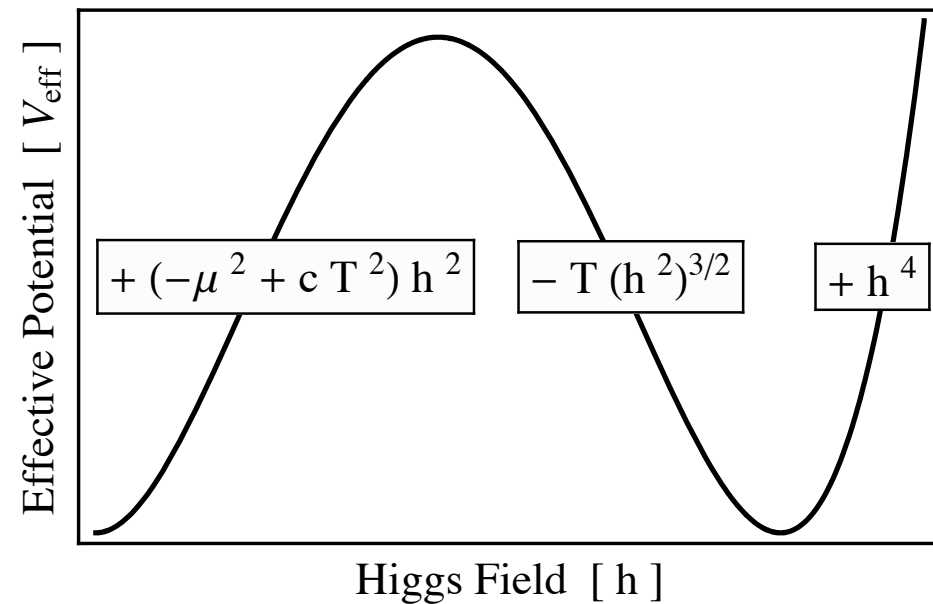
2nd order Phase Transition

Left is good, further  $v_c/T_c > 1$

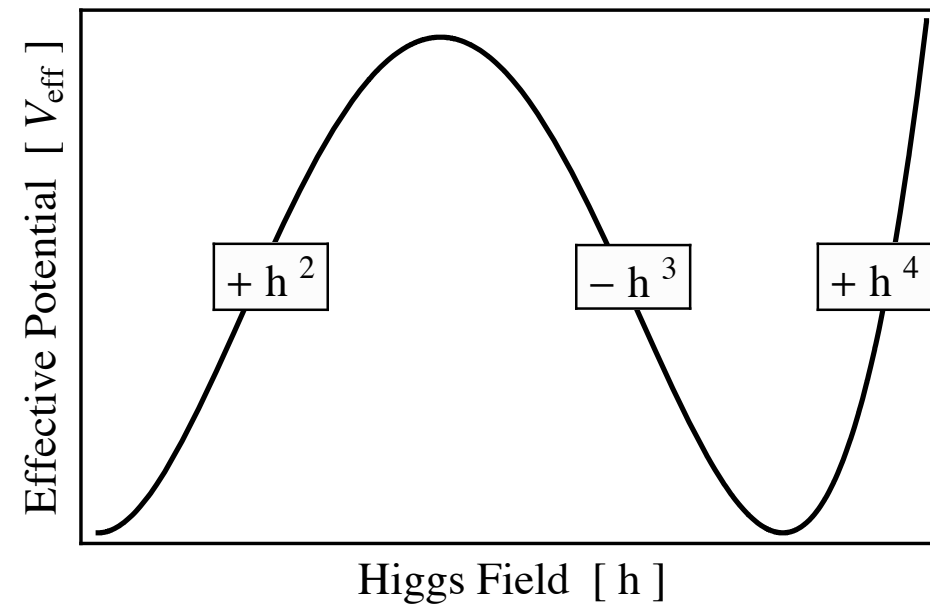


# Extensions to Higgs

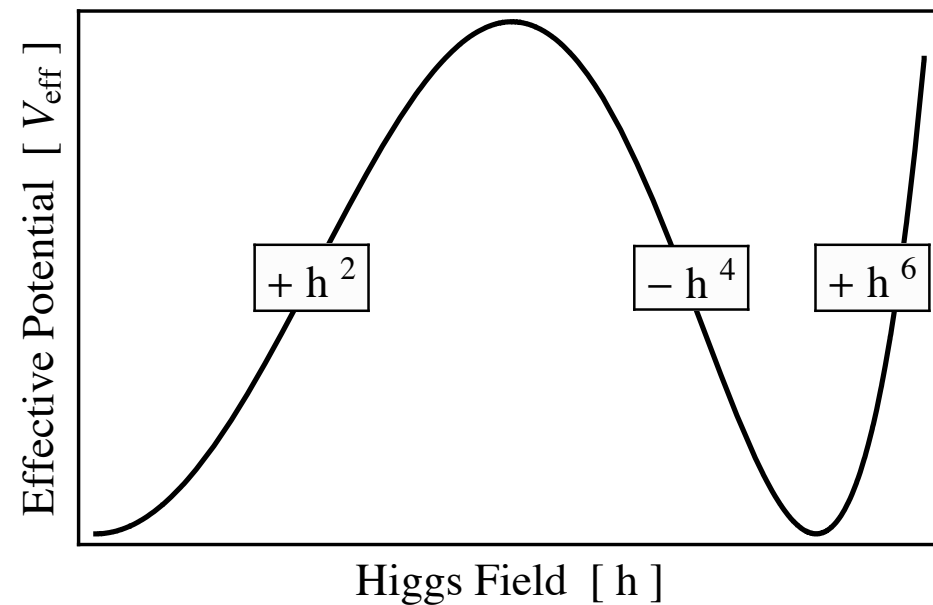
I. Thermally (BEC) Driven



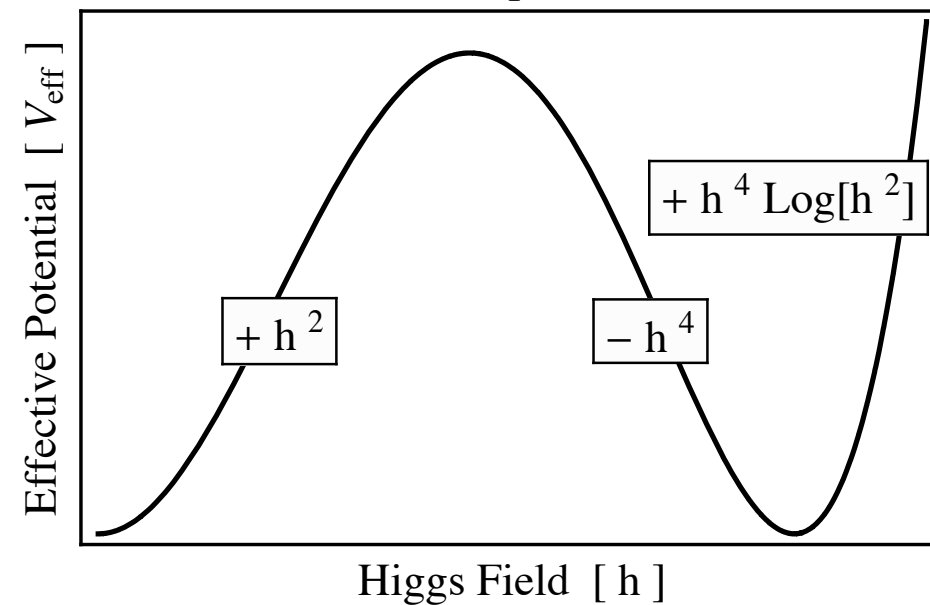
IIA. Tree-Level (Ren.) Driven



IIB. Tree-Level (Non-Ren.) Driven



III. Loop Driven



Chung et.al.1209.1819

# Why is Type 1 special?



- only type where Temperature produces the cubic coupling.
- All other types affect the Higgs tri-linear coupling
- Requires precision thermal field theory.

# High temperature approximation

## Ring induced phase transition

- add new singlet :  $\Delta L = -\frac{1}{2}\mu_s^2 s^2 + \frac{1}{2}\lambda_{hs}h^2 s^2 + \frac{1}{4}\lambda_s s^4$
- now, at high T,  $V_{CW}^{T \neq 0} = -\frac{T^4}{90} + \frac{T^4}{24} \frac{M^2}{T^2} - \frac{T^4}{12\pi} \left( \frac{M^3}{T^3} \right)$
- replacing,  $M^2 \rightarrow M^2 + \Pi$  for an extra singlet coupled to the Higgs,
- you get  $(M_s^2 + \Pi)^{3/2} = (-\mu_s^2 + \lambda_{hs}h^2 + \Pi)^{3/2}$
- and then  $(M_s^2 + \Pi)^{3/2} = \cancel{(-\mu_s^2 + \lambda_{hs}h^2 + \Pi)^{3/2}} = \lambda_{hs}^{(3/2)} h^3$

# Wait What?

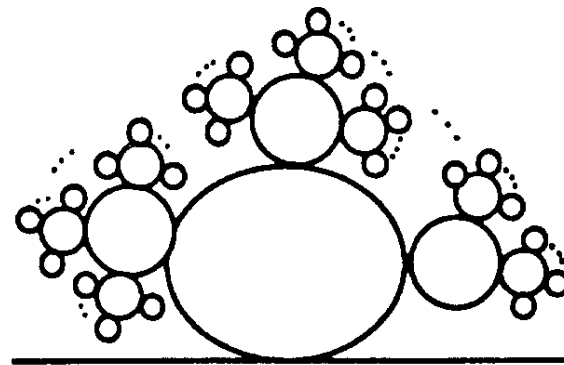
- How is high  $T$  limit valid?  $T \sim$  EW scale and so are all masses
- In fact typically the extra scalar is more massive
- Mass is  $h$  dependent.
- regions where  $M$  is small: approximation valid
- regions where  $M \sim T$ , thermal mass small for small coupling

$$\Pi = \frac{\lambda_{hs}}{2} T^2$$

# Problems with

$$\Pi = \frac{\lambda_{hs}}{2} T^2$$

- Thermal mass doesn't decouple as  $M_s$  becomes massive
- Thermal mass seems to be  $h$  independent
- Super-Daisy terms not taken into account.



# New Work

# What we did

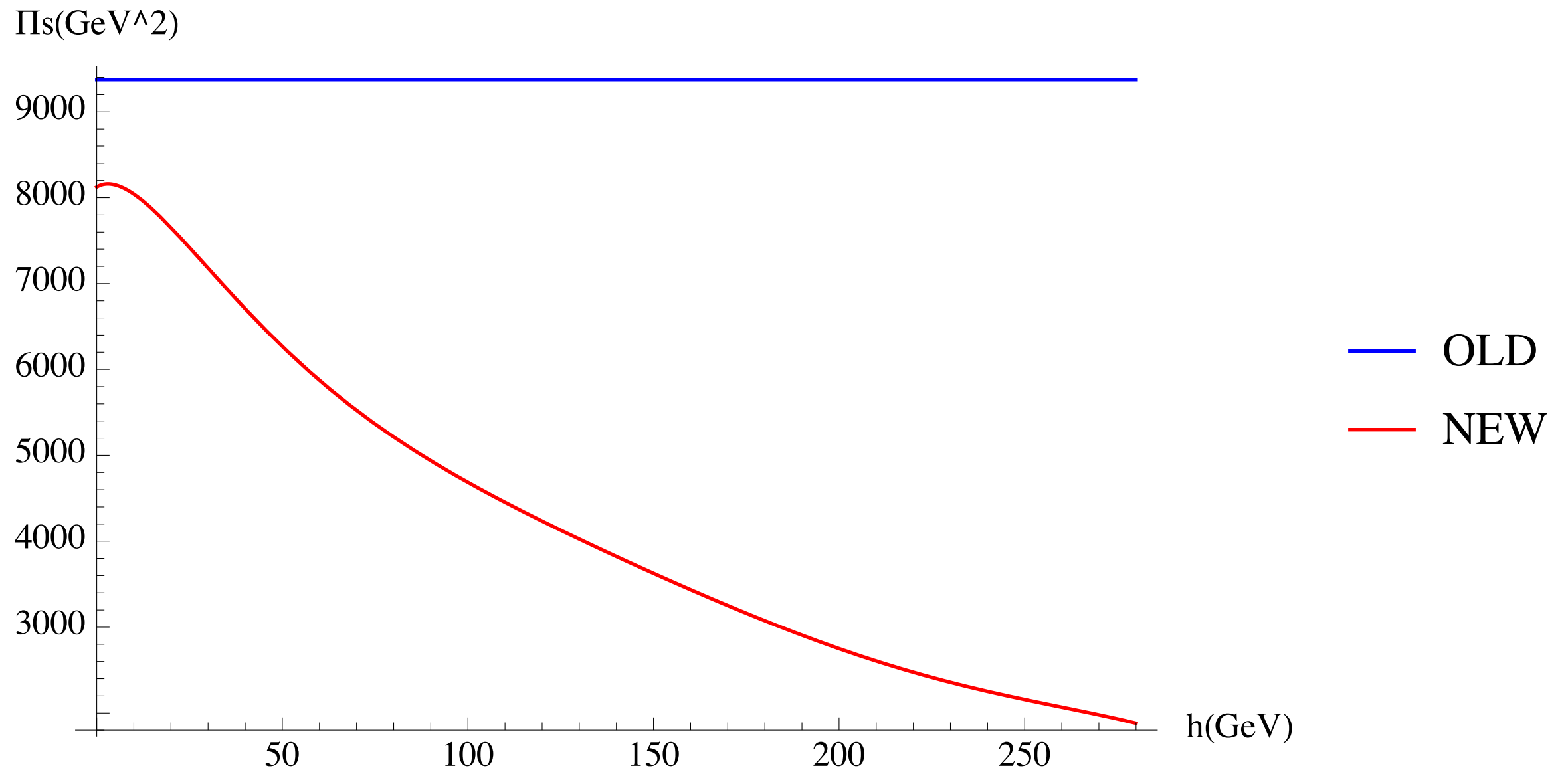
- Computed thermal mass accurately.(no high-T expansion)
- How about new thermal mass after substitution?

$$\Pi_{\text{super}} = \frac{dV'_T}{dh} [M^2 \rightarrow M^2 + \Pi_{\text{super}}]$$

- Solved iteratively to take into account super-daisy

# RESULTS

## Old vs New Thermal Mass





# Procedure

- Account for accurate thermal mass in potential
- Cool down to find critical temperature
- is  $S$  still stable?, i.e.  $M_s^2 + \Pi_s > 0$
- is  $v_c/T_c > 1$

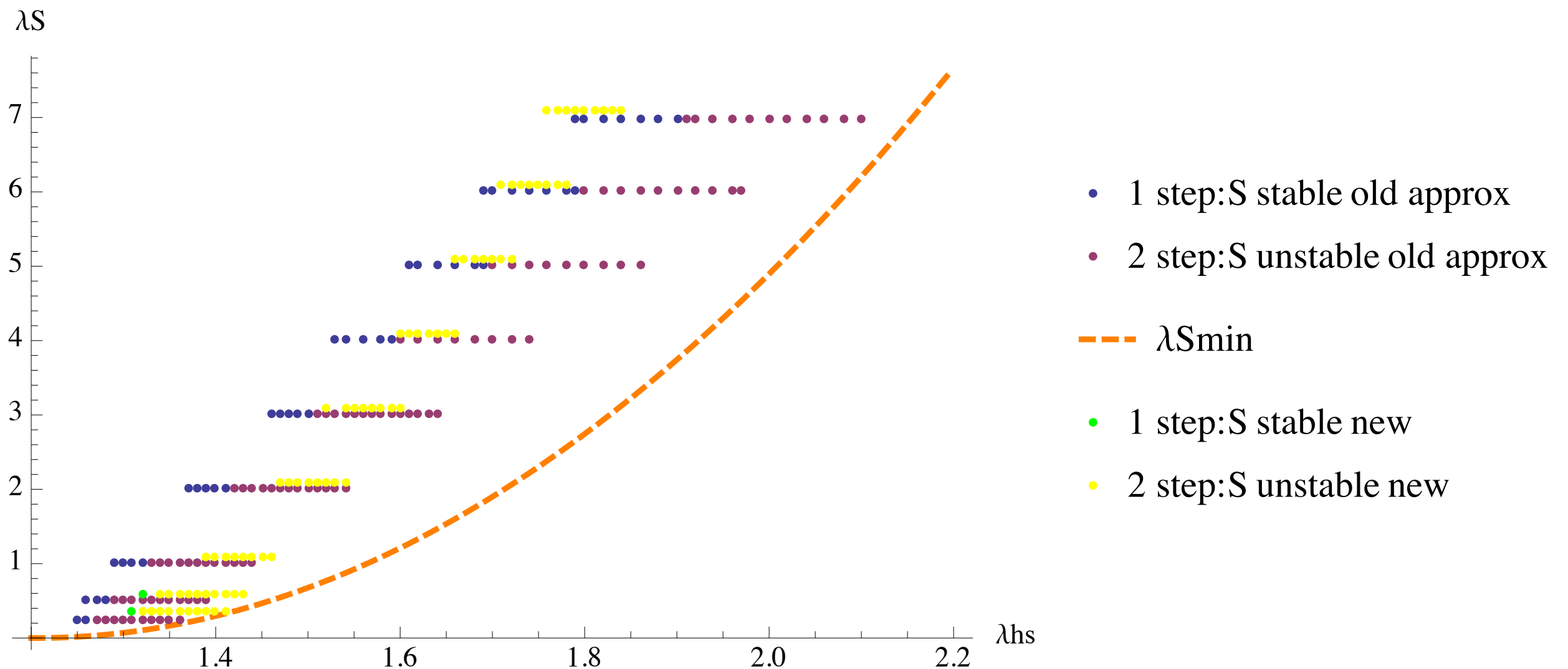
# RESULTS



Parameter space where ring induced 1st-order phase transition feasible



$$M_S = 270 \text{ GeV}$$



# RESULTS-IDM



Parameter space where ring induced 1st-order phase transition feasible



	$M_H$	$M_A$	$M_{H^{+-}}$	$\lambda_L$	$\lambda_T$	$v_c/T_c(\text{old})$	$v_c/T_c(\text{new})$
<b>BM1</b>	66	300	300	0.01	0.01	1.5	1.1
<b>BM2</b>	200	400	400	0.01	0.01	1.5	1.2
<b>BM3</b>	5	265	265	-0.006	0.01	1.3	1.0

for  $v_c/T_c(\text{old})$  refer 1504.05949

# Summary

- FTFT required to handle EWPT
- in some regimes high  $T$  approx not valid
- Full iteration based computation the way out
- Leads to drastically reduced parameter space for thermally induced phase transition

The Ring has awoken,  
its heard its masters call

